

## **MICROFLUIDIC DEVICE WITH ULTRAPHOBIC SURFACES**

### **RELATED APPLICATIONS**

This application claims the benefit of U.S. Provisional Patent Application Serial No. 60/462963, entitled "Ultrapophobic Surface for High Pressure Liquids", filed April 15, 2003, hereby fully incorporated herein by reference. This application further claims the benefit of U.S. Utility Patent Application Serial No. 10/454,742 entitled "Fluid Handling Component With Ultrapophobic Surfaces", filed June 3, 2003, also hereby fully incorporated herein by reference.

### **FIELD OF THE INVENTION**

This invention relates generally to microfluidic devices, and more specifically to a microfluidic device having ultraphobic fluid contact surfaces.

### **BACKGROUND OF THE INVENTION**

There has been much recent interest and effort directed to developing and using microfluidic devices. Microfluidic devices have already found useful application in printing devices and in so-called "lab-on-a-chip" devices, wherein complex chemical and biochemical reactions are carried out in microfluidic devices. The very small volumes of liquid needed for reactions in such a system enables increased reaction response time, low sample volume, and reduced reagent cost. It is anticipated that a myriad of further applications will become evident as the technology is refined and developed.

A significant factor in the design of a microfluidic device is the resistance to fluid movement imposed by contact of fluid with surfaces in the microscopic channels of the device. In order to overcome this resistance, higher fluid pressures are required within the device. In turn, fluid flow rates through the device may be limited by the amount of pressure that can be tolerated by the device or the process that the device supports. In addition, pressure losses through microscopic flow channels may vary greatly due to the characteristics of surfaces in the flow channel.

What is needed in the industry is a microfluidic device with fluid flow channels having predictable and optimal levels of resistance to fluid flow.

### SUMMARY OF THE INVENTION

The invention substantially meets the needs of the industry for a microfluidic device having fluid flow channels with predictable and optimal levels of fluid flow resistance. In the invention, all or any portion of the fluid flow channels of any microfluidic device are provided with durable ultraphobic fluid contact surfaces. The ultraphobic surface generally includes a substrate portion with a multiplicity of projecting regularly shaped microscale or nanoscale asperities disposed in a regular array so that the surface has a predetermined contact line density measured in meters of contact line per square meter of surface area equal to or greater than a critical contact line density value “ $\Lambda_L$ ” determined according to the formula:

$$\Lambda_L = \frac{-P}{\gamma \cos(\theta_{a,0} + \omega - 90^\circ)},$$

where  $P$  is a predetermined maximum expected fluid pressure value within the fluid flow channel,  $\gamma$  is the surface tension of the liquid,  $\theta_{a,0}$  is the experimentally measured true advancing contact angle of the liquid on the asperity material in degrees, and  $\omega$  is the asperity rise angle, and so that the ratio of the cross-sectional dimension of the asperities to the spacing dimension of the asperities is less than or equal to 0.1.

The asperities may be formed in or on the substrate material itself or in one or more layers of material disposed on the surface of the substrate. The asperities may be any regularly or irregularly shaped three dimensional solid or cavity and may be disposed in any regular geometric pattern.

The invention may also include process of making a microfluidic device including steps of forming at least one microscopic fluid flow channel in a body, the fluid flow channel having a fluid contact surface, and disposing a multiplicity of substantially uniformly shaped asperities in a substantially uniform pattern on the fluid contact surface. Each asperity may have a cross-sectional dimension and an asperity rise angle relative to the fluid contact surface. The asperities may be spaced apart by a substantially uniform spacing dimension and positioned so that the surface has a contact line density measured in meters of contact line per square meter of surface area equal to or greater than a critical contact line density value " $\Lambda_L$ " determined according to the formula:

$$\Lambda_L = \frac{-P}{\gamma \cos(\theta_{a,0} + \omega - 90^\circ)}$$

where  $P$  is a predetermined maximum expected fluid pressure value within the fluid flow channel,  $\gamma$  is the surface tension of the liquid,  $\theta_{a,0}$  is the experimentally measured true advancing contact angle of the liquid on the asperity material in degrees, and  $\omega$  is the asperity rise angle. The ratio of the cross-sectional dimension of the asperities to the spacing dimension of the asperities is preferably less than or equal to 0.1 and most preferably less than or equal to 0.01.

The asperities may be formed using photolithography, or using nanomachining, microstamping, microcontact printing, self-assembling metal colloid monolayers, atomic force microscopy nanomachining, sol-gel molding, self-assembled monolayer directed patterning, chemical etching, sol-gel stamping, printing with colloidal inks, or by disposing a layer of carbon nanotubes on the substrate. The process may further include the step of determining a critical asperity height value " $Z_c$ " in meters according to the formula:

$$Z_c = \frac{d (1 - \cos (\theta_{a,0} + \omega - 180^\circ))}{2 \sin (\theta_{a,0} + \omega - 180^\circ)}$$

where  $d$  is the least distance in meters between adjacent asperities,  $\theta_{a,0}$  is the true advancing contact angle of the liquid on the surface in degrees, and  $\omega$  is the asperity rise angle in degrees.

It is anticipated that fluid flow channels in a microfluidic device having ultraphobic fluid contact surfaces will exhibit sharply reduced resistance to fluid flow, leading to greatly improved device efficiencies, lower intradevice pressures and improved fluid flow throughput. The

ultraphobic surfaces will be durable, and capable of exhibiting predictable ultraphobic properties under fluid pressures up to the maximum design pressure.

BRIEF DESCRIPTION OF THE DRAWINGS

5        Fig. 1 is a perspective, greatly enlarged view of an ultraphobic surface according to the present invention;

      Fig. 1a is a schematic view of a liquid slug in a flow channel;

      Fig. 1b is an exploded view of a microfluidic device according to the present invention;

      Fig. 1c is a cross-sectional view of an alternative embodiment of a microfluidic device  
10    according to the present invention;

      Fig. 2 is a top plan view of a portion of the surface of Fig. 1;

      Fig. 3 is a side elevation view of the surface portion depicted in Fig. 2;

      Fig. 4 is a partial top plan view of an alternative embodiment of an ultraphobic surface according to the present invention wherein the asperities are arranged in a hexagonal array;

15        Fig. 5 is a side elevation view of the alternative embodiment of Fig. 4;

      Fig. 6 is a side elevation view depicting the deflection of liquid suspended between asperities;

      Fig. 7 is a side elevation view depicting a quantity of liquid suspended atop asperities;

      Fig. 8 is a side elevation view depicting the liquid contacting the bottom of the space  
20    between asperities;

Fig. 9 is a side elevation view of a single asperity in an alternative embodiment of an ultraphobic surface according to the present invention wherein the asperity rise angle is an acute angle;

Fig. 10 is a side elevation view of a single asperity in an alternative embodiment of an ultraphobic surface according to the present invention wherein the asperity rise angle is an obtuse angle;

Fig. 11 a partial top plan view of an alternative embodiment of an ultraphobic surface according to the present invention wherein the asperities are cylindrical and are arranged in a rectangular array;

Fig. 12 is a side elevation view of the alternative embodiment of Fig. 11;

Fig. 13 is a table listing formulas for contact line density and linear fraction of contact for a variety of asperity shapes and arrangements;

Fig. 14 is a side elevation view of an alternative embodiment of an ultraphobic surface according to the present invention;

Fig. 15 is a top plan view of the alternative embodiment of Fig. 14;

Fig. 16 is a top plan view of a single asperity in an alternative embodiment of an ultraphobic surface according to the present invention; and

Fig. 17 is a graphical representation for a specific ultraphobic surface and liquid of the relationship between asperity spacing ( $y$ ) and maximum pressure ( $P$ ) for various values of the  $x/y$  ratio.

DETAILED DESCRIPTION OF THE INVENTION

For the purposes of the present application, the term “microfluidic device” refers broadly to any other device or component that may be used to contact, handle, transport, contain, process, or convey a fluid, wherein the fluid flows through one or more fluid flow channels of microscopic dimensions. For the purposes of the present application, “microscopic” means dimensions of 500  $\mu\text{m}$  or less. “Fluid flow channel” broadly refers to any channel, conduit, pipe, tube, chamber, or other enclosed space of any cross-sectional shape used to handle, transport, contain, or convey a fluid. The term “fluid contact surface” refers broadly to any surface or portion thereof of a fluid flow channel that may be in contact with a fluid.

It is known that the physical characteristics of the fluid contact surfaces of fluid handling components have an effect on friction of the fluid with the components. Generally, for example, smoother surfaces reduce friction, while rougher surfaces increase friction. Also, surfaces made from materials resistant to wetting, such as PTFE or other engineered polymers, exhibit relatively lower fluid friction. Surfaces that are resistant to wetting by liquids are referred to as “phobic” surfaces. Such surfaces may be known as hydrophobic where the liquid is water, and lyophobic relative to other liquids. If a surface resists wetting to an extent that a small droplet of water or other liquid exhibits a very high stationary contact angle with the surface (greater than about 120 degrees), if the surface exhibits a markedly reduced propensity to retain liquid droplets, or if a liquid-gas-solid interface exists at the surface when completely submerged in liquid, the surface may be referred to as an “ultrahydrophobic” or “ultralyophobic” surface. For

the purposes of this application, the term ultraphobic is used to refer generally to both ultrahydrophobic and ultralyophobic surfaces.

Friction between a liquid and a surface may be dramatically lower for an ultraphobic surface as opposed to a conventional surface. As a result, ultraphobic surfaces are extremely desirable for reducing resistance to fluid flow due to surface resistance forces, especially in microfluidic applications.

It is now well known that surface roughness has a significant effect on the degree of surface wetting. It has been generally observed that, under some circumstances, roughness can cause liquid to adhere more strongly to the surface than to a corresponding smooth surface. Under other circumstances, however, roughness may cause the liquid to adhere less strongly to the rough surface than the smooth surface. In some circumstances, the surface may be ultraphobic. Such an ultraphobic surface generally takes the form of a substrate member with a multiplicity of microscale to nanoscale projections or cavities, referred to herein as “asperities”.

Generally, the pressure ( $\Delta P_{total}$ ) for moving a liquid slug through a horizontal flow channel at a given velocity may be divided into components of viscous forces, surface forces, and gravity forces (head) so that:

$$\Delta P_{total} = \Delta P_{viscous} + \Delta P_{surface} + \Delta P_{gravity}. \quad (1)$$

A horizontally oriented cylindrical flow channel 110 is depicted in cross-section in Fig. 1a. The cylindrical flow channel 110 is defined by a channel wall 115 having a fluid contact surface 120. A liquid slug 100 is depicted within flow channel 110. Liquid slug 100 has a forward interface 130 with fluid 132 and a rear interface 140 with fluid 142. It will be



appreciated that fluid 132 and fluid 142 may be in gaseous or liquid form. For horizontally oriented cylindrical flow channel 110, the general relation given in equation (1) above may be more specifically expressed as:

5

$$\Delta P_{total} = \frac{8\mu L v}{R^2} + \frac{2\gamma(\cos \theta_r - \cos \theta_a)}{R}, \quad (2)$$

where  $\mu$  is the viscosity of the liquid,  $L$  is the length of liquid slug 100,  $v$  is the velocity with which liquid slug 100 is moving,  $R$  is the cross-sectional radius of the cylindrical flow channel 110,  $\gamma$  is the surface tension of the liquid in liquid slug 100,  $\theta_r$  is the actual receding contact angle of the rear interface 140 of liquid slug 100 with surface 120 of flow channel 110 and  $\theta_a$  is the actual advancing contact angle of the forward interface 130 of liquid slug 100 with surface 120 of flow channel 110. Similar specific equations are described in the prior art for flow channels of non-cylindrical flow channels.

For a liquid slug 100 having one or more interfaces 130, 140, contacting surface 120 in a microscopic flow channel 110, surface forces will be dominant due to the miniscule dimensions of liquid slug 100. The viscous component of the forces may essentially be neglected. Thus, the pressure ( $\Delta P$ ) for moving liquid slug 100 through a horizontal microscopic cylindrical flow channel 110 effectively becomes:

20

$$\Delta P = \frac{2\gamma(\cos \theta_r - \cos \theta_a)}{R}. \quad (3)$$

By minimizing these surface forces through the use of ultraphobic flow channel surfaces according to the present invention, significant reductions in the pressure for moving a liquid slug through the flow channel may be achieved.

5 A microfluidic device 10 according to the present invention is depicted in a greatly enlarged, exploded view in Fig. 1b. Device 10 generally includes a body 11 with a rectangular flow channel 12 formed therein. Body 11 generally includes a main portion 13 and a cover portion 14. Flow channel 12 is defined on three sides by inwardly facing surfaces 15 on main portion 13 and on a fourth side by an inwardly facing surface 16 on cover portion 14. Surfaces 15 and surface 16 together define channel wall 16a. According to the present invention, all or  
10 any desired portion of channel wall 16a may be provided with an ultraphobic fluid contact surface 20. Although a two-piece configuration with rectangular flow channel is depicted in Fig. 1b, it will of course be readily appreciated that microfluidic device 10 may be formed in any other configuration and with virtually any other flow channel shape or configuration, including a one piece body 11 with a cylindrical, polygonal, or irregularly shaped flow channel formed  
15 therein.

An alternative embodiment of a microfluidic device is depicted in cross-section in Fig. 1c. In this embodiment, body 200 is formed in one integral piece. Cylindrical flow channel 202 is defined within body 200, and has a channel wall 204 presenting ultraphobic fluid contact surface 20 facing into flow channel 202.

20 A greatly enlarged view of ultraphobic fluid contact surface 20 according to the invention is depicted in Fig. 1. The surface 20 generally includes a substrate 22 with a multiplicity of

projecting asperities 24. As further described herein, substrate 22 may be a portion of body 11 or may be a separate layer of material on body 11. Asperities 24 are typically formed from substrate 22 as also further described herein. Each asperity 24 has a plurality of sides 26 and a top 28. Each asperity 24 has a width dimension, annotated "x" in the figures, and a height dimension, annotated "z" in the figures.

As depicted in Figs. 1-3, asperities 24 are disposed in a regular rectangular array, each asperity spaced apart from the adjacent asperities by a spacing dimension, annotated "y" in the figures. The angle subtended by the top edge 30 of the asperities 24 is annotated  $\phi$ , and the rise angle of the side 26 of the asperities 24 relative to the substrate 22 is annotated  $\omega$ . The sum of the angles  $\phi$  and  $\omega$  is 180 degrees.

Generally, ultraphobic fluid contact surface 20 will exhibit ultraphobic properties when a liquid-solid-gas interface is maintained at the surface. As depicted in Fig. 7, if liquid 32 contacts only the tops 28 and a portion of the sides 26 proximate top edge 30 of asperities 24, leaving a space 34 between the asperities filled with air or other gas, the requisite liquid-solid-gas interface is present. The liquid may be said to be "suspended" atop and between the top edges 30 of the asperities 24.

As will be disclosed hereinbelow, the formation of the liquid-solid-gas interface depends on certain interrelated geometrical parameters of the asperities 24 and the properties of the liquid, and the interaction of the liquid with the solid surface. According to the present invention, the geometrical properties of asperities 24 may be selected so that the surface 20 exhibits ultraphobic properties at any desired liquid pressure.

Referring to the rectangular array of Figs. 1-3, surface 20 may be divided into uniform areas 36, depicted bounded by dashed lines, surrounding each asperity 24. The area density of asperities ( $\delta$ ) in each uniform area 36 may be described by the equation:

$$\delta = \frac{1}{y^2}, \quad (4)$$

where  $y$  is the spacing between asperities measured in meters.

For asperities 24 with a square cross-section as depicted in Figs. 1-3, the length of perimeter ( $p$ ) of top 28 at top edge 30:

$$p = 4x, \quad (5)$$

where  $x$  is the asperity width in meters.

Perimeter  $p$  may be referred to as a “contact line” defining the location of the liquid-solid-gas interface. The contact line density ( $\Lambda$ ) of the surface, which is the length of contact line per unit area of the surface, is the product of the perimeter ( $p$ ) and the area density of asperities ( $\delta$ ) so that:

$$\Lambda = p \delta. \quad (6)$$

For the rectangular array of square asperities depicted in Figs. 1-3:

$$\Lambda = 4x/y^2. \quad (7)$$

5           A quantity of liquid will be suspended atop asperities 24 if the body forces ( $F$ ) due to gravity acting on the liquid are less than surface forces ( $f$ ) acting at the contact line with the asperities. Body forces ( $F$ ) associated with gravity may be determined according to the following formula:

$$10 \quad F = \rho gh, \quad (8)$$

where ( $\rho$ ) is the density of the liquid, ( $g$ ) is the acceleration due to gravity, and ( $h$ ) is the depth of the liquid. Thus, for example, for a 10 meter column of water having an approximate density of 1000 kg/m<sup>3</sup>, the body forces ( $F$ ) would be:

$$15 \quad F = (1000 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(10 \text{ m}) = 9.8 \times 10^4 \text{ kg/m}^2\text{-s}.$$

Surface forces ( $f$ ) depend on the surface tension of the liquid ( $\gamma$ ), its apparent contact angle with the side 26 of the asperities 24 with respect to the vertical  $\theta_s$ , the contact line density of the asperities ( $\Lambda$ ) and the apparent contact area of the liquid ( $A$ ):

20

$$f = - \Lambda A \gamma \cos \theta_s. \quad (9)$$

The true advancing contact angle ( $\theta_{a,0}$ ) of a liquid on a given solid material is defined as the largest experimentally measured stationary contact angle of the liquid on a surface of the material having essentially no asperities. The true advancing contact angle is readily measurable by techniques well known in the art.

Suspended drops on a surface with asperities exhibit their true advancing contact angle value ( $\theta_{a,0}$ ) at the sides of the asperities. The contact angle with respect to the vertical at the side of the asperities ( $\theta_s$ ) is related to the true advancing contact angle ( $\theta_{a,0}$ ) by  $\phi$  or  $\omega$  as follows:

$$\theta_s = \theta_{a,0} + 90^\circ - \phi = \theta_{a,0} + \omega - 90^\circ. \quad (10)$$

By equating  $F$  and  $f$  and solving for contact line density  $\Lambda$ , a critical contact line density parameter  $\Lambda_L$  may be determined for predicting ultraphobic properties in a surface:

$$\Lambda_L = \frac{-\rho g h}{\gamma \cos(\theta_{a,0} + \omega - 90^\circ)}, \quad (11)$$

where  $\rho$  is the density of the liquid,  $g$  is the acceleration due to gravity,  $h$  is the depth of the liquid, the surface tension of the liquid ( $\gamma$ ),  $\omega$  is the rise angle of the side of the asperities

relative to the substrate in degrees, and  $(\theta_{a,0})$  is the experimentally measured true advancing contact angle of the liquid on the asperity material in degrees.

If  $\Lambda > \Lambda_L$ , the liquid will be suspended atop the asperities 24, producing an ultraphobic surface. Otherwise, if  $\Lambda < \Lambda_L$ , the liquid will collapse over the asperities and the contact  
5 interface at the surface will be solely liquid/solid, without ultraphobic properties.

It will be appreciated that by substituting an appropriate value in the numerator of the equation given above, a value of critical contact line density may be determined to design a surface that will retain ultraphobic properties at any desired amount of pressure. The equation may be generalized as:

$$\Lambda_L = \frac{-P}{\gamma \cos(\theta_{a,0} + \omega - 90^\circ)}, \quad (12)$$

where P is the maximum pressure under which the surface must exhibit ultraphobic properties in kilograms per square meter,  $\gamma$  is the surface tension of the liquid in Newtons per meter,  $\theta_{a,0}$  is the  
15 experimentally measured true advancing contact angle of the liquid on the asperity material in degrees, and  $\omega$  is the asperity rise angle in degrees.

It is generally anticipated that a surface 20 formed according to the above relations will exhibit ultraphobic properties under any liquid pressure values up to and including the value of P used in equation (12) above. The ultraphobic properties will be exhibited whether the surface is  
20 submerged, subjected to a jet or spray of liquid, or impacted with individual droplets.

Once the value of critical contact line density is determined, the remaining details of the geometry of the asperities may be determined according to the relationship of  $x$  and  $y$  given in the equation for contact line density. In other words, the geometry of the surface may be determined by choosing the value of either  $x$  or  $y$  in the contact line equation and solving for the other variable.

The tendency of the ultraphobic surface 20 to repel droplets of liquid so that the droplets rest on the surface at very high contact angles, may be best expressed in terms of contact angle hysteresis ( $\Delta\theta$ ), which is the difference between the advancing and receding contact angles for a liquid droplet on the surface. Generally, lower values of contact angle hysteresis correspond to a relatively greater repellency characteristic of the surface. Contact angle hysteresis for a surface may be determined according to the following equation:

$$\Delta\theta = \lambda_p(\Delta\theta_0 + \omega), \quad (13)$$

where ( $\lambda_p$ ) is the linear fraction of contact along the asperities, ( $\Delta\theta_0$ ) is the difference between the true advancing contact angle ( $\theta_{a,0}$ ) and the true receding contact angle ( $\theta_{r,0}$ ) for the surface material, and ( $\omega$ ) is the rise angle of the asperities. For a rectangular array of square asperities:

$$\lambda_p = x/y. \quad (14)$$

Equations for determining for surfaces having other geometries are given in Fig. 13. For droplets of liquid on the surface, the actual advancing contact angle of the surface may be determined according to the equation:

$$\theta_a = \lambda_p(\theta_{a,0} + \omega) + (1 - \lambda_p)\theta_{air}, \quad (15)$$

and the actual receding contact angle may be determined according to the equation:



$$\theta_r = \lambda_p \theta_{r,0} + (1 - \lambda_p) \theta_{air}. \quad (16)$$

It will be readily appreciated by examining the relations given hereinabove that relatively lower values of  $\lambda_p$ ,  $\omega$ ,  $x/y$ , and  $\Lambda$  lead to relatively improved repellency for the surface, and that relatively higher values of each of these same parameters lead to relatively improved ability of the surface to suspend a column of liquid. As a result, it will generally be necessary to strike a balance in selecting values for these parameters if a surface with good repellency and suspension characteristics is desired.

The above equations may also be used to plot the relationship for given liquid properties between asperity spacing ( $y$ ) and maximum pressure ( $P$ ) for various values of  $x/y$ . Such plots, an example of which is depicted in Fig. 17, may serve as useful design tools as is demonstrated in the example given hereinbelow.

The liquid interface deflects downwardly between adjacent asperities by an amount  $D_1$  as depicted in Fig. 6. If the amount  $D_1$  is greater than the height ( $z$ ) of the asperities 24, the liquid will contact the substrate 22 at a point between the asperities 24. If this occurs, the liquid will be drawn into space 34, and collapse over the asperities, destroying the ultraphobic character of the surface. The value of  $D_1$  represents a critical asperity height ( $Z_c$ ), and is determinable according to the following formula:

$$D_1 = Z_c = \frac{d \left( 1 - \cos \left( \theta_{a,0} + \omega - 180^\circ \right) \right)}{2 \sin \left( \theta_{a,0} + \omega - 180^\circ \right)}, \quad (17)$$

where ( $d$ ) is the least distance between adjacent asperities at the contact line,  $\omega$  is the asperity rise angle, and  $\theta_{a,0}$  is the experimentally measured true advancing contact angle of the liquid on the asperity material. The height ( $z$ ) of asperities 24 must be at least equal to, and is preferably greater than, critical asperity height ( $Z_c$ ).

5 Although in Figs. 1-3 the asperity rise angle  $\omega$  is 90 degrees, other asperity geometries are possible. For example,  $\omega$  may be an acute angle as depicted in Fig. 9 or an obtuse angle as depicted in Fig. 10. Generally, it is preferred that  $\omega$  be between 80 and 130 degrees.

It will also be appreciated that a wide variety of asperity shapes and arrangements are possible within the scope of the present invention. For example, asperities may be polyhedral, 10 cylindrical as depicted in Figs. 11-12, cylindroid, or any other suitable three dimensional shape. In addition, various strategies may be utilized to optimize contact line density of the asperities. As depicted in Figs. 14 and 15, the asperities 24 may be formed with a base portion 38 and a head portion 40. The larger perimeter of head portion 40 at top edge 30 increases the contact line density of the surface. Also, features such as recesses 42 may be formed in the asperities 24 15 as depicted in Fig. 16 to increase the perimeter at top edge 30, thereby increasing contact line density. The asperities may also be cavities formed in the substrate.

The asperities may be arranged in a rectangular array as discussed above, in a polygonal array such as the hexagonal array depicted in Figs. 4-5, or a circular or ovoid arrangement. The asperities may also be randomly distributed so long as the critical contact line density is 20 maintained, although such a random arrangement may have less predictable ultraphobic properties, and is therefore less preferred. In such a random arrangement of asperities, the

critical contact line density and other relevant parameters may be conceptualized as averages for the surface. In the table of Fig. 13, formulas for calculating contact line densities for various other asperity shapes and arrangements are listed.

Generally, the substrate material may be any material upon which micro or nano scale  
5 asperities may be suitably formed. The asperities may be formed directly in the substrate material itself, or in one or more layers of other material deposited on the substrate material, by photolithography or any of a variety of suitable methods. Direct extrusion may be used to form asperities in the form of parallel ridges. Such parallel ridges are most desirably oriented transverse to the direction fluid flow. A photolithography method that may be suitable for  
10 forming micro/nanoscale asperities is disclosed in PCT Patent Application Publication WO 02/084340, hereby fully incorporated herein by reference.

Other methods that may be suitable for forming asperities of the desired shape and spacing include nanomachining as disclosed in U.S. Patent Application Publication No. 2002/00334879, microstamping as disclosed in U.S. Patent No. 5,725,788, microcontact printing  
15 as disclosed in U.S. Patent No. 5,900,160, self-assembled metal colloid monolayers, as disclosed in U.S. Patent 5,609,907, microstamping as disclosed in U.S. Patent No. 6,444,254, atomic force microscopy nanomachining as disclosed in U.S. Patent 5,252,835, nanomachining as disclosed in U.S. Patent No. 6,403,388, sol-gel molding as disclosed in U.S. Patent No. 6,530,554, self-assembled monolayer directed patterning of surfaces, as disclosed in U.S. Patent No. 6,518,168,  
20 chemical etching as disclosed in U.S. Patent No. 6,541,389, or sol-gel stamping as disclosed in U.S. Patent Application Publication No. 2003/0047822, all of which are hereby fully

incorporated herein by reference. Carbon nanotube structures may also be usable to form the desired asperity geometries. Examples of carbon nanotube structures are disclosed in U.S. Patent Application Publication Nos. 2002/0098135 and 2002/0136683, also hereby fully incorporated herein by reference. Also, suitable asperity structures may be formed using known methods of printing with colloidal inks. Of course, it will be appreciated that any other method by which micro/nanoscale asperities may be accurately formed may also be used.

Generally, it is most desirable to optimize the repellency characteristics of the ultraphobic flow channel surfaces in order to minimize contact of the liquid slug with the flow channel surfaces, thereby also minimizing the resulting surface forces. As explained hereinabove, repellency characteristics of the surface may be optimized by selecting relatively lower values for  $\lambda_p$ ,  $\omega$ ,  $x/y$ , or  $\Lambda$ , while still ensuring that the surface has a sufficient critical contact line density value ( $\Lambda_L$ ) to ensure that the surface has ultraphobic properties at the maximum pressure expected to be encountered in the flow channel. For best flow channel performance, the  $x/y$  ratio for the asperity geometry should be less than about 0.1 and most preferably about 0.01.

A method of optimizing a microscopic flow channel for repellency characteristics may be illustrated by the following examples:

#### EXAMPLE 1:

A cylindrical microscopic flow channel is to be formed in a silicon body to produce a microfluidic device. An ultraphobic surface is to be provided on the inwardly facing walls of the microscopic flow channel according to the present

invention. The ultraphobic surface will consist of an array of square posts ( $\omega = 90^\circ$ ) disposed on the walls of the channel. The channel walls will also be coated with organosilane so that the channel has the following dimensions and characteristics:

5

$$R = 1\mu\text{m}$$

$$\theta_{a,0} = 110^\circ$$

$$\theta_{r,0} = 90^\circ$$

10

A water slug in the flow channel has the following dimensions and characteristics:

$$\gamma = 0.073 \text{ N/m}$$

$$L = 0.1 \text{ mm}$$

$$v = 0.1 \text{ mm/s}$$

15

If the flow channel has smooth fluid contact surfaces so that the actual advancing and receding contact angles of the slug ( $\theta_a, \theta_r$ ) are substantially equal to the true advancing and receding contact angles for the fluid contact surface material, the pressure required to move the liquid slug through the smooth flow channel may be calculated as:

20

$$\Delta P = \frac{2\gamma(\cos \theta_r - \cos \theta_a)}{R} = \frac{2(0.073)(\cos 90 - \cos 110)}{0.000001} \approx 5 \times 10^4 \text{ Pa}$$

Repellancy of the fluid contact surface is optimized by selecting a small  $x/y$  ratio so as to increase the actual advancing and receding contact angles of the water at the fluid contact surface:

$$\text{Select } x/y = \lambda_p = 0.01$$

So that:

$$\theta_a = \lambda_p (\theta_{a,0} + \omega) + (1 - \lambda_p) \theta_{air} = 180^\circ$$

and:

$$\theta_r = \lambda_p \theta_{r,0} + (1 - \lambda_p) \theta_{air} = 179^\circ$$

The pressure for moving the liquid slug through the flow channel having ultraphobic fluid contact surfaces becomes:

$$\Delta P = \frac{2\gamma(\cos \theta_r - \cos \theta_a)}{R} = \frac{2(0.073)(\cos 179 - \cos 180)}{0.000001} \approx 1 \times 10^2 \text{ Pa}$$

The remaining geometric details of the surface may then be determined as follows using the relations given above:

$$\Lambda_L = \frac{-\Delta P}{\gamma \cos(\theta_{a,0} + \omega - 90^\circ)} = \frac{-100}{0.073 \cos(110 + 90 - 90)} \approx 4000 \text{ m}^{-1}$$

Referring to Fig. 17, which is a plot of the relationship between asperity spacing (y) and maximum pressure (P) for various values of x/y, with water as the liquid and with values of  $\theta_{a,0}$  and  $\theta_{r,0}$  consistent with the organosilane coated silicon material, it may be determined that y should be about  $1 \times 10^{-5}$  m or 10  $\mu\text{m}$  for a maximum pressure of 100 Pa and an x/y ratio of 0.01. Accordingly:

$$x = 0.01(y) = 0.01(1 \times 10^{-5} \text{ m}) = 1 \times 10^{-7} \text{ m or } 100 \text{ nm}$$

Next, solving for  $Z_c$ :

$$Z_c = \frac{d(1 - \cos(\theta_{a,0} + \omega - 180^\circ))}{2 \sin(\theta_{a,0} + \omega - 180^\circ)} = \frac{(10\mu\text{m} - 0.1\mu\text{m})(1 - \cos(110^\circ + 90^\circ - 180^\circ))}{2 \sin(110^\circ + 90^\circ - 180^\circ)} \approx 0.9\mu\text{m}$$

Thus, if the square asperities are placed on the fluid contact surfaces in the flow channel in a rectangular array, they should have a cross-sectional dimension of about 100nm, should be spaced at about 10  $\mu\text{m}$  apart and should be at least 0.9  $\mu\text{m}$  in height.

#### EXAMPLE 2:

Assume a cylindrical microscopic flow channel in PFA plastic having the following dimensions and characteristics:

$$R = 10 \mu\text{m}$$

$$\theta_{a,0} = 110^\circ$$

$$\theta_{r,0} = 90^\circ$$

5

Assume also a water slug in the flow channel:

$$\gamma = 0.073 \text{ N/m}$$

$$L = 1 \text{ mm}$$

$$v = 0.1 \text{ mm/s}$$

10

Again, if the flow channel has smooth fluid contact surfaces so that the actual advancing and receding contact angles of the slug ( $\theta_a, \theta_r$ ) are substantially equal to the true advancing and receding contact angles for the fluid contact surface material, the pressure required to move the liquid slug through the smooth flow channel may be calculated as:

15

$$\Delta P = \frac{2\gamma(\cos \theta_r - \cos \theta_a)}{R} = \frac{2(0.073)(\cos 90 - \cos 110)}{0.000010} \approx 5 \times 10^3 \text{ Pa}$$

20

An array of square posts ( $\omega = 90^\circ$ ) is to be disposed on the fluid contact surface of the flow channel so as to form an ultraphobic surface.



Select  $x/y = \lambda_p = 0.1$

So that:

5

$$\theta_a = \lambda_p (\theta_{a,0} + \omega) + (1 - \lambda_p) \theta_{air} = 180^\circ$$

and:

10

$$\theta_r = \lambda_p \theta_{r,0} + (1 - \lambda_p) \theta_{air} = 171^\circ$$

The pressure for moving the liquid slug through the flow channel having ultraphobic fluid contact surfaces becomes:

15

$$\Delta P = \frac{2\gamma(\cos \theta_r - \cos \theta_a)}{R} = \frac{2(0.073)(\cos 171 - \cos 180)}{0.000010} \approx 180 Pa$$

The remaining geometric details of the surface may then be determined as follows using the relations given above:

$$\Lambda_L = \frac{-\Delta P}{\gamma \cos(\theta_{a,0} + \omega - 90^\circ)} = \frac{-180 Pa}{0.073 \cos(110 + 90 - 90)} \approx 7200$$

20

Referring to Fig. 17, which is a plot of the relationship between asperity spacing (y) and maximum pressure (P) for various values of x/y, with water as the liquid

and with values of  $\theta_{a,0}$  and  $\theta_{r,0}$  consistent with PFA material, it may be determined that  $y$  should be about  $1 \times 10^{-5}$  m or  $10 \mu\text{m}$  for a maximum pressure of 100 Pa and an  $x/y$  ratio of 0.01. Accordingly:

$$x = 0.1(y) = 0.1(10 \mu\text{m}) = 1 \mu\text{m}$$

5 Next, solving for  $Z_c$ :

$$Z_c = \frac{d (1 - \cos (\theta_{a,0} + \omega - 180^\circ))}{2 \sin (\theta_{a,0} + \omega - 180^\circ)} = \frac{(10 \mu\text{m} - 1 \mu\text{m}) (1 - \cos (110^\circ + 90^\circ - 180^\circ))}{2 \sin (110^\circ + 90^\circ - 180^\circ)} \approx 0.8 \mu\text{m}$$

Thus, if the square asperities are placed on the fluid contact surfaces in the flow channel in a rectangular array, they should have a cross-sectional dimension of about  $1 \mu\text{m}$ , should be spaced at about  $10 \mu\text{m}$  apart and should be at least  $0.8 \mu\text{m}$  in height.

10

It will be readily appreciated by those of skill in the art that the above disclosed method may be used to determine the optimal asperity spacing and geometry for an ultraphobic fluid contact surface in a microscopic flow channel for any desired liquid and flow channel surface material.

15 Additional objects, advantages, and novel features of the invention will be set forth in part in the description which follows, and in part will become apparent to those skilled in the art upon examination of the following or may be learned by practice of the invention. The objects and advantages of the invention may be realized and attained by means of the instrumentalities and combinations particularly pointed out in the appended claims.